

Print your name: \_\_\_\_\_

Answer each question completely. You must justify your answers to get credit. Even a correct answer with no justification will get no credits.

1. Consider the ordinary differential equation  $x^2 y' = y$ .

(a) What is the order of the ODE? (No justification needed.)

(1 pt)

1

(b) Verify that  $y(x) = Ce^{-1/x}$  is a solution to the ODE for any value of the constant  $C$ .

(6 pts)

$$y' = Ce^{-1/x} \cdot \frac{1}{x^2}$$

$$\text{LHS} = x^2 y' = x^2 \cdot \left( Ce^{-1/x} \cdot \frac{1}{x^2} \right)$$

$$= Ce^{-1/x} = y = \text{RHS} \quad \checkmark$$

(c) Find a solution to the initial-value problem  $x^2 y' = y$ ,  $y(1) = 1$ . (You may use part (b) even if you did not solve it.)

(3 pts)

$$y(1) = Ce^{-1/1} = Ce^{-1} = 1$$

$$\Leftrightarrow C = e$$

Answer:  $y(x) = e \cdot e^{-1/x} = e^{1-1/x}$ .