

Print your name: _____

Answer each question completely. You must justify your answers to get credit. Even a correct answer with no justification will get no credits.

Consider the series $\sum_{n=1}^{\infty} \frac{1}{n^{\frac{3}{2}} + 1}$.

1. Thinking about what you have learned so far, what do you **think** the behavior of this series is? No justification needed. (Answer this question before the next questions; you are **not** allowed to change your answer.) (1 pts)

Convergent Divergent
 (It looks like the p-series w/ $p = \frac{3}{2} > 1$.)

2. Apply the divergence test to check for convergence or divergence. What is the conclusion? (3 pts)

$$\lim_{n \rightarrow \infty} \frac{1}{n^{\frac{3}{2}} + 1} = 0$$

INCONCLUSIVE

3. Apply the ratio test to check for convergence or divergence. What is the conclusion? (3 pts)

$$\begin{aligned} \rho &= \lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \lim_{n \rightarrow \infty} \left| \frac{1/(n+1)^{\frac{3}{2}} + 1}{1/n^{\frac{3}{2}} + 1} \right| \\ &= \lim_{n \rightarrow \infty} \frac{n^{\frac{3}{2}} + 1}{(n+1)^{\frac{3}{2}} + 1} = \lim_{n \rightarrow \infty} \frac{1 + 1/n^{\frac{3}{2}}}{(1 + \frac{1}{n})^{\frac{3}{2}} + 1/n^{\frac{3}{2}}} = 1 \end{aligned}$$

INCONCLUSIVE

4. Apply the comparison test to check for convergence or divergence. What is the conclusion? (Hint: Your answer in problem 1 is important to find a candidate series to compare with.) (3 pts)

$$\sum_{n=1}^{\infty} \frac{1}{n^{\frac{3}{2}} + 1} \leq \sum_{n=1}^{\infty} \frac{1}{n^{\frac{3}{2}}}$$

p-series
w/ $p = \frac{3}{2} > 1$
which is convergent.

Therefore $\sum_{n=1}^{\infty} \frac{1}{n^{\frac{3}{2}} + 1}$ is convergent.